



Name: _____

Date: _____

Student Exploration: Solving Linear Systems (Standard Form)

Vocabulary: elimination method, solution, standard form, substitution method, system of linear equations

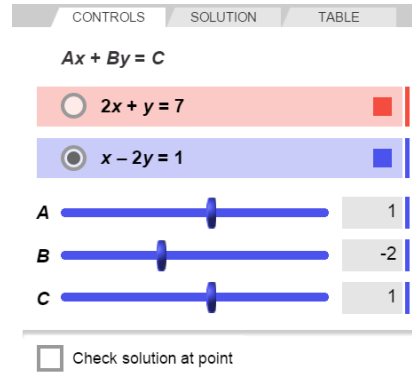
Prior Knowledge Questions (Do these BEFORE using the Gizmo.)

1. The point (3, 1) is on the line whose equation is $2x + y = c$. What is the value of c ? _____
2. The point (3, 1) is also on the line whose equation is $x - 2y = d$. What is the value of d ? _____
3. Do you think the lines have any other points in common? _____ Explain. _____

Gizmo Warm-up

The equations $2x + y = 7$ and $x - 2y = 1$ form a **system of linear equations** in **standard form** ($Ax + By = C$, where A , B , and C are real numbers, and A and B are not both zero). In the *Solving Linear Systems (Standard Form)* Gizmo, you can use graphing or algebra to solve such systems.

On the **CONTROLS** tab, select the top equation. Set **A** to 2, **B** to 1, and **C** to 7 to graph $2x + y = 7$. Then select the bottom equation. Set **A** to 1, **B** to -2 , and **C** to 1 to graph $x - 2y = 1$. (To quickly set the value of a slider, type the number into the text box to the right of the slider and press **Enter**.)



1. The **solution** of an equation contains the value or values that make the equation true. Select **Check solution at point**. Drag the green point to (5, 2).

Is (5, 2) a solution of both $2x + y = 7$ and $x - 2y = 1$? _____ Explain. _____

2. Drag the green point to (1, 5). Is (1, 5) a solution of both equations? _____
3. Drag the green point to the purple point. Is (3, 1) a solution of both equations? _____



Activity B: Using elimination	<u>Get the Gizmo ready:</u> <ul style="list-style-type: none"> On the CONTROLS tab, turn off Check solution at point. 	
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1. One way to solve a system of linear equations algebraically is to use the **elimination method**. Consider the system of equations $x - y = 3$ and $2x + y = 6$.

A. The second equation above states that $2x + y$ is equal to 6. So, if you take the first equation ($x - y = 3$) and add $2x + y$ to the left side, and add 6 to the right side, you are adding equal quantities to each side. This means you still have a true equation.

In the space to the right, add the two equations and solve the resulting equation. Notice what happens to y .

$$\begin{array}{r} x - y = 3 \\ 2x + y = 6 \\ \hline \end{array}$$

Why do you think this method is called elimination?

B. In the space to the right, substitute the x -value you found above into either equation and solve for y .

In the Gizmo, graph the equations on the **CONTROLS** tab. Then select the **SOLUTION** tab and choose **Elimination** to check your work.

2. Consider the system of equations $2x + 3y = 4$ and $x + 4y = -3$.

A. Multiply each side of the equation $x + 4y = -3$ by -2 . _____

B. How do you think the solution of the system $2x + 3y = 4$ and $x + 4y = -3$ compares to that of the system $2x + 3y = 4$ and $-2x - 8y = 6$? _____

Explain. _____

C. In the space to the right, add $-2x - 8y = 6$ to $2x + 3y = 4$. Then solve the resulting equation.

D. In the space to the right, solve for x .
Check your answer in the Gizmo.

(Activity B continued on next page)



Activity B (continued from previous page)

3. Consider the system of equations $3x + 2y = -7$ and $2x - 5y = 8$.

A. Suppose you want to add the equations to eliminate y . By what numbers should you multiply each equation? _____

B. Multiply each equation by the numbers above. Then solve the system. Show your work to the right.

C. At what point do you think the graphs of these equations intersect? (_____, _____)

Check your answer in the Gizmo.

4. Consider the system of equations $4x - 7y = -4$ and $4x - 7y = 5$.

A. Do you think this system has a solution? _____ Explain. _____

B. Select the **CONTROLS** tab and graph this system. How are the lines related?

C. Use elimination to solve this system. Show your work. Check in the Gizmo.

D. How does this result tell you there is no solution? _____

5. Graph the system of equations $x - 2y = -2$ and $3x - 6y = -6$ in the Gizmo.

A. How are the graphs related? _____

B. Use elimination to solve this system. Show your work. Check in the Gizmo.

C. How does this result tell you there are infinitely many solutions? _____



Activity C: Practice solving systems	<u>Get the Gizmo ready:</u>	<input type="radio"/> $4x + y = -2$
	<ul style="list-style-type: none"> Select the CONTROLS tab. 	<input checked="" type="radio"/> $4x + 5y = -6$

1. Consider the system of equations $4x + y = -2$ and $4x + 5y = -6$.

A. Would you use the substitution method or the elimination method to solve this

system algebraically? _____ Why? _____

B. Use the method of your choice to solve the system in the space to the right. Then graph the system in the Gizmo. Select the **SOLUTION** tab and check your answer.

2. You can use the substitution method or the elimination method to solve any system of linear equations. However, in some cases, one method might be a little easier than the other.

Fill in the table below with a system of linear equations you would solve using substitution, and a system you would solve using elimination. Explain why you would use the chosen method to solve each system. Then solve each system and check in the Gizmo.

	Easier method: Substitution	Easier method: Elimination
System of equations		
Explanation (Why is this method easier?)		
Solution		

(Activity C continued on next page)



Activity C (continued from previous page)

3. Use substitution or elimination to solve each system. Show your work below each system. Check your answer in the Gizmo.

A. $x + y = -1$
 $x - y = 3$ Solution: _____

D. $2x + 5y = -6$
 $3x + 2y = 2$ Solution: _____

B. $3x - 2y = 3$
 $x + 2y = 1$ Solution: _____

E. $6x - 8y = 3$
 $6x - 8y = -3$ Solution: _____

C. $4x + y = 3$
 $3x - 2y = 5$ Solution: _____

F. $2x + 4y = -4$
 $x + 2y = -2$ Solution: _____

