



## Vocabulary: Logarithmic Functions

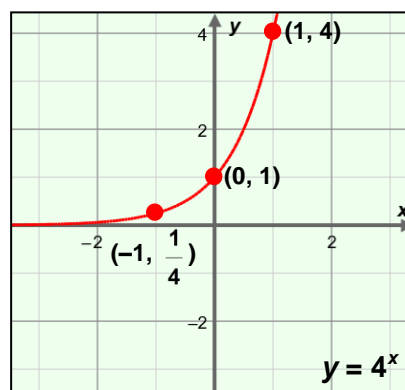


### Vocabulary

- **Asymptote** – a line that a curve approaches as  $x$  or  $y$  goes to infinity.
- **Base** – a number or expression raised to an exponent.
  - The logarithmic function  $y = \log_b(x)$  is said to have base  $b$ , because  $y = \log_b(x)$  written in exponential form is  $b^y = x$ .
- **Domain** – the set of all  $x$ -values of a relation or function.
- **Exponent** – a number, written to the right of and just above a number or expression, that indicates how many times the number or expression is multiplied by itself.

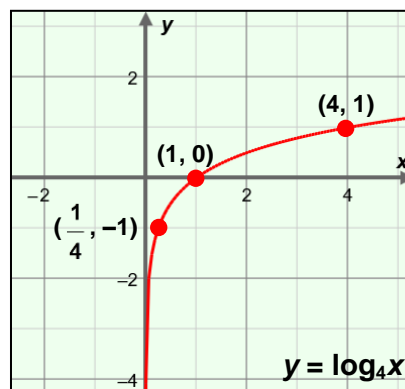
- **Exponential function** – a function of the form  $y = a \cdot b^{kx}$ , where  $a \neq 0$ ,  $b > 0$ , and  $b \neq 1$ .

- For example, the function  $y = 4^x$ , graphed to the right, is exponential.
  - Some “key points” on the graph of  $y = 4^x$  are  $(-1, \frac{1}{4})$ ,  $(0, 1)$ ,  $(1, 4)$ ,  $(2, 16)$ , etc.
  - For  $y = 4^x$ , every time  $x$  increases by 1,  $y$  is multiplied by a factor of 4.



- **Inverse function** – a function that “reverses” or “undoes” another function.
  - If the point  $(x, y)$  lies on the graph of the original function, then  $(y, x)$  lies on the graph of its inverse function.
  - The graph of an inverse function is the graph of the original function reflected across the line  $y = x$ .
- **Logarithmic function** – the inverse of an exponential function.

- The logarithmic function  $y = \log_b(x)$  is the inverse of  $y = b^x$ , where  $b > 0$  and  $b \neq 1$ .
- For example, the function  $y = \log_4(x)$ , graphed to the right, is logarithmic.
  - “Key points” on the graph of  $y = \log_4(x)$  include  $(\frac{1}{4}, -1)$ ,  $(1, 0)$ ,  $(4, 1)$ ,  $(16, 2)$ , etc.
  - The value of  $\log_4(1) = 0$  because  $4^0 = 1$ .



- **Range** – the set of all  $y$ -values of a relation or function.

